

Algebra I

7-2

Solving Systems: The Substitution Method

Solve by the substitution method.

$$\begin{aligned}
 1) \quad & y = 6x \\
 & x + y = 28 \\
 & x + (6x) = 28 \\
 & 7x = 28 \\
 & x = 4 \\
 & y = 6(4) \\
 & y = 24
 \end{aligned}$$

After we solve for one of the two variables, we SUBSTITUTE its value in one of the two original equations. Choose whichever seems easiest to solve for the remaining variable.

Answers should be written as a point in alphabetical order.

$$\{(4, 24)\}$$

$$\begin{aligned}
 2) \quad & 3x + 1 = y \\
 & 2x + 3y = 25
 \end{aligned}$$

$$\begin{aligned}
 2x + 3(3x + 1) &= 25 \\
 2x + 9x + 3 &= 25 \\
 11x + 3 - 3 &= 25 - 3 \\
 11x &= 22 \\
 x &= 2
 \end{aligned}$$

$$\begin{aligned}
 3(2) + 1 &= y \\
 6 + 1 &= y \\
 7 &= y
 \end{aligned}$$

$$\{(2, 7)\}$$

$$\begin{aligned}
 3) \quad & 2r + 3s = 0 \\
 & r + 5 = 6s
 \end{aligned}$$

$$\begin{aligned}
 r + 5 - 5 &= 6s - 5 \\
 r &= 6s - 5
 \end{aligned}$$

$$\begin{aligned}
 2(6s - 5) + 3s &= 0 \\
 12s - 10 + 3s &= 0 \\
 15s - 10 + 10 &= 0 + 10 \\
 15s &= 10 \\
 s &= \frac{2}{3}
 \end{aligned}$$

$$\begin{aligned}
 r &= 6\left(\frac{2}{3}\right) - 5 \\
 r &= 4 - 5 = -1
 \end{aligned}$$

$$\left\{-1, \frac{2}{3}\right\}$$

$$4) \quad c = d + 8$$

$$\begin{aligned}
 \left(\frac{c}{5} = d + 4\right) 5 \\
 c = 5d + 20
 \end{aligned}$$

$$\begin{aligned}
 (5d + 20) - d &= 8 \\
 4d + 20 &= 8 \\
 4d + 20 - 20 &= 8 - 20 \\
 4d &= -12 \\
 d &= -3
 \end{aligned}$$

$$\begin{aligned}
 c &= 5(-3) + 20 \\
 c &= -15 + 20 \\
 c &= 5
 \end{aligned}$$

$$\{(5, -3)\}$$

Assignment:

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4-16 even,

20-28 even,

31-33 all.